



## Reducing the Complexity of Separation Dynamics using the Computational Analysis through Finite Volume Schemes in Multi-Component Gradient Elution Chromatography.



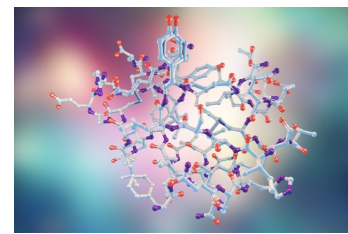
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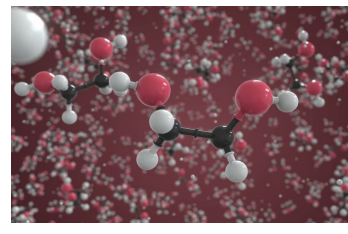
### Why Chromatographic Technologies Require?

#### World of Chromatographic Science:

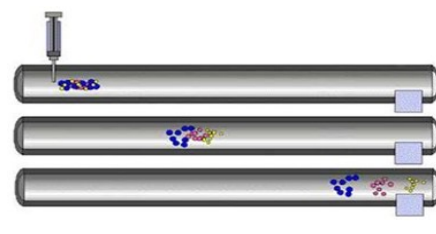
**Chromatography:** separation technique and high purity and productivity



Evaluating HPLC

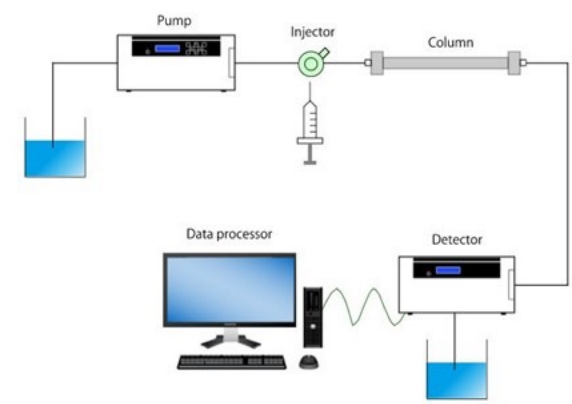


Separation of PEO

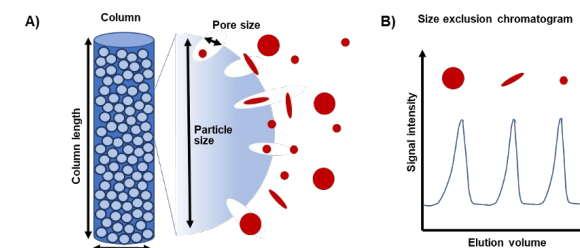


Movement of components

#### EXPERIMENTAL SYSTEM:



Experimental process



2 Nobel Prizes!



### What is Application?



- Pharmaceutical Company: Identify amount of chemicals in new product.
- Environmental Agency: Determine the level of pollutants in water supply.
- Biological application: Separate and identify amino acids, carbohydrates, fatty acids and other natural substances that are the parts of any mixture.
- Law Enforcement: Comparing crime scene samples to suspect samples.
- Manufacturing Plant: To purify a chemical that needed to make new product.

### Mathematical Model:

#### Non-linear LKM Model :

$$\frac{\partial c_i}{\partial t} + u \frac{\partial c_i}{\partial z} = D_{z,i} \frac{\partial^2 c_i}{\partial z^2} - F \frac{\partial q_i}{\partial t}, \quad \frac{\partial q_i}{\partial t} = k_{m,i}(\phi)(q_i^*(\phi(t,z)) - q_i), \quad i = 1, \dots, N_c$$

$$c_i(z, 0) = q_i(z, 0) = 0, \quad \text{and } c_i(0, t) \begin{cases} c_{i, \text{inj}}, & \text{if } 0 < t < t_{\text{inj}} \\ 0, & \text{if } t > t_{\text{inj}} \end{cases}, \quad \frac{\partial c_i(L, t)}{\partial z} = 0$$

#### Transport Model:

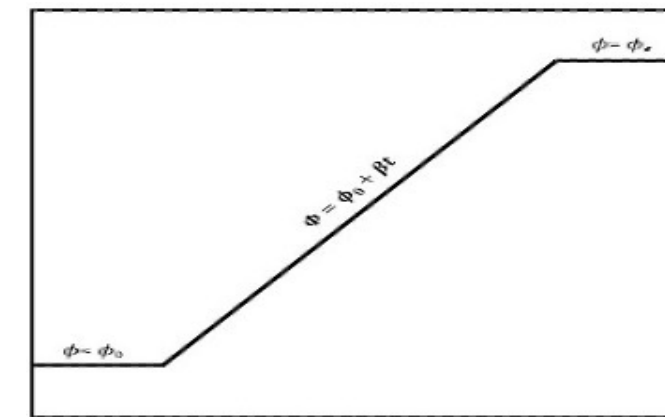
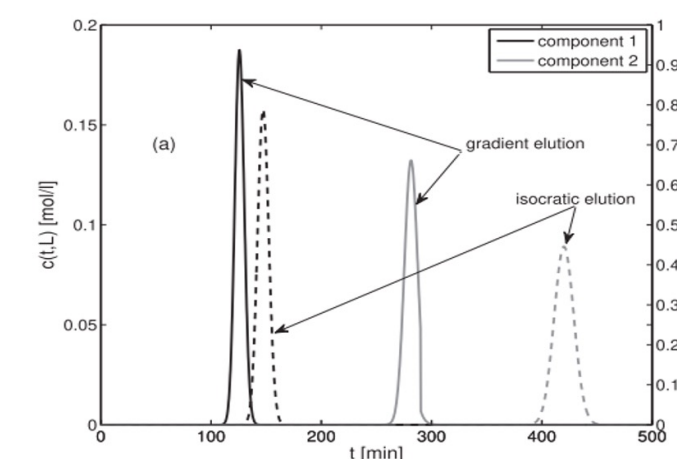
A transport model is used to describe gradient elution in liquid chromatography. The ideal model is:

$$a \frac{\partial \phi}{\partial t} + u \frac{\partial \phi}{\partial z} = 0, \quad \phi(0, z) = \phi_0, \quad z \in [0, L] \text{ and } \phi(t, 0) = \begin{cases} \phi_0 & \text{if } t < t_s \\ \phi(t - t_s) & \text{if } t_s \leq t \leq t_e \\ \phi_e & \text{if } t > t_e \end{cases}$$

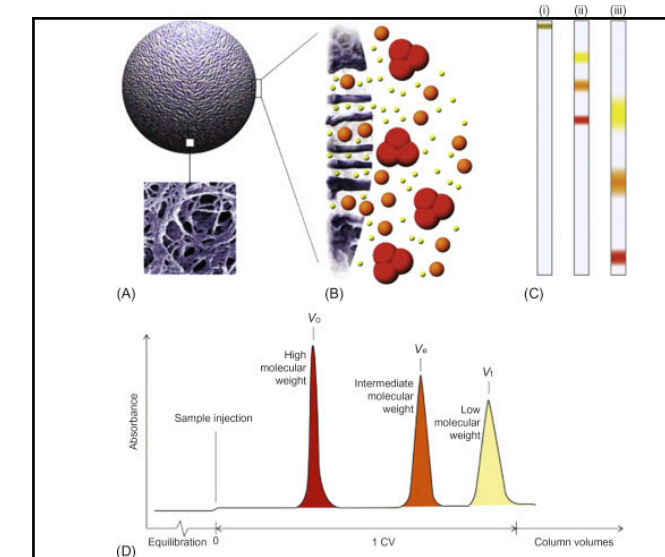
#### Types of Elution:

**Gradient Elution:** Mobile phase composition that changing steadily during process of chromatographic run.  
**Isocratic Elution:** Mobile phase composition that is not changing during the process of chromatographic run.

#### Parameters and Computer Simulation:

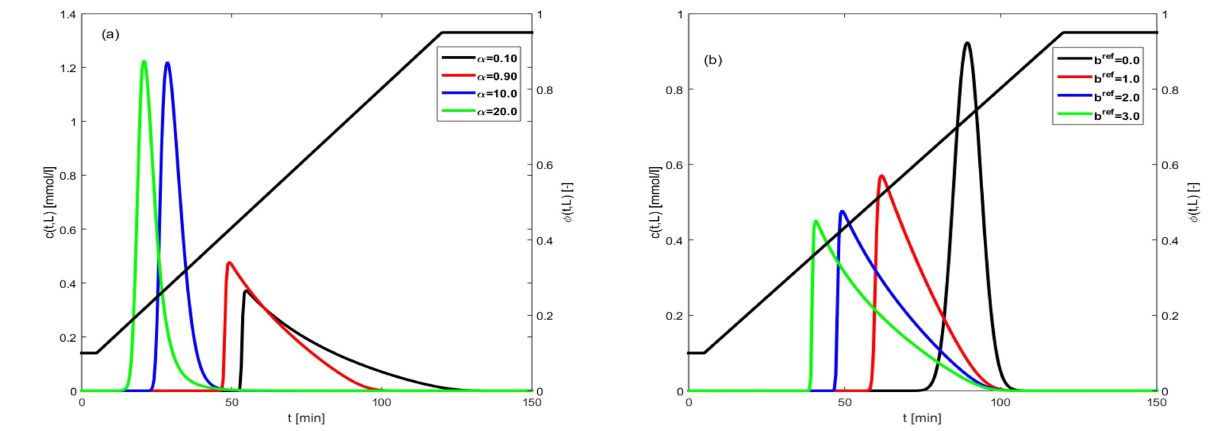


Symbol	Quantity	Value
$L$	Column Length	10 cm
$u$	Interstitial velocity	$1.0 \frac{\text{cm}}{\text{min}}$
$k_{Hr}$	Henry's constant	7
$\alpha$	Solvent strength	0.90
$b^{bref}$	Nonlinearity coefficient	2
$c_{inj}$	Injected concentration	$10 \text{ min}^{-1}$
$k_L$	Mass transfer coefficient	$1 \frac{\text{mol}}{\text{l}}$

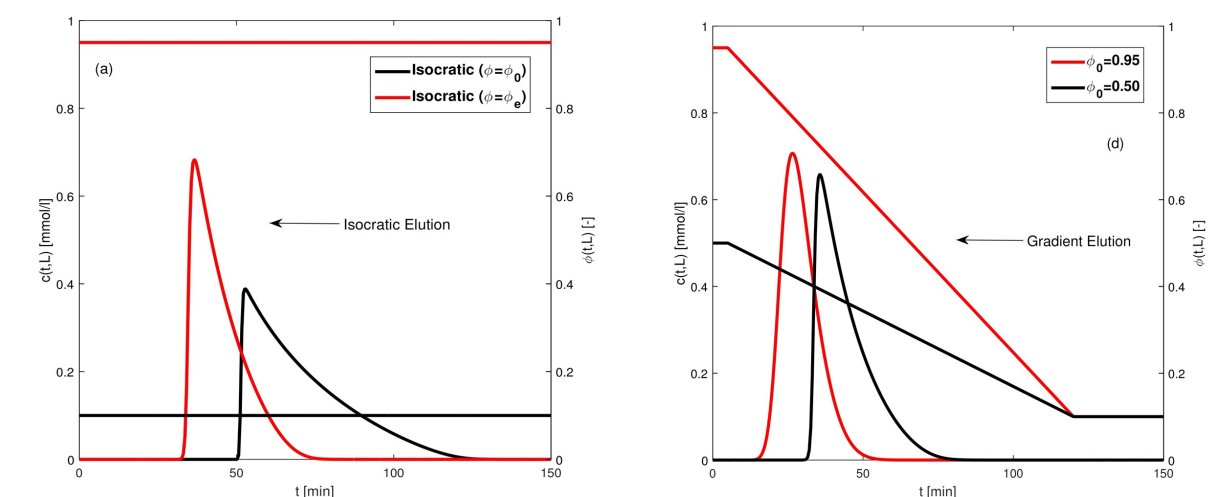


### RESULTS OF SIMULATION & EXPERIMENTS:

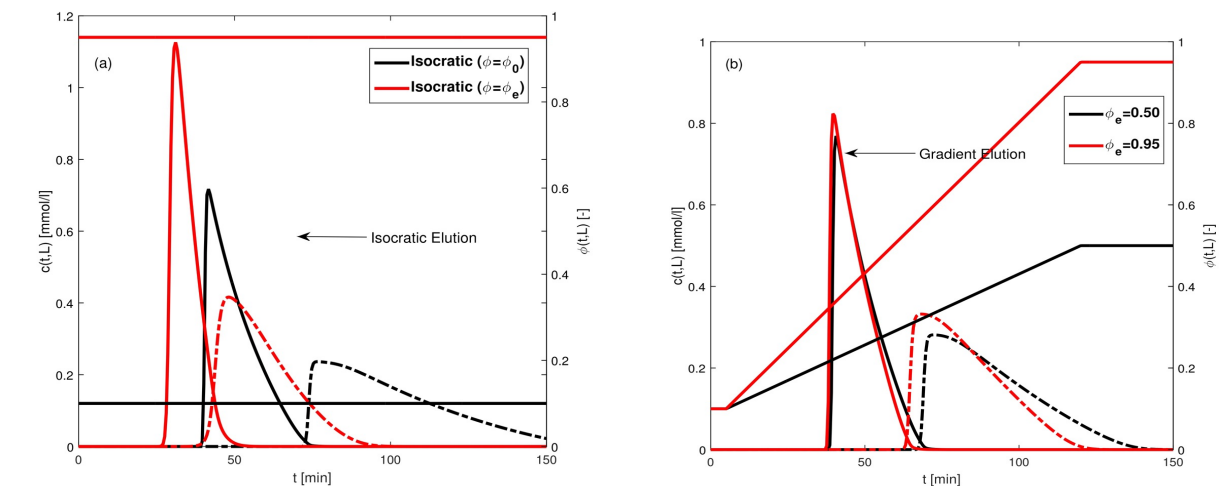
#### One component profiles:



#### One component elution profiles:



#### Two component elution profiles:



### SUMMARY AND OUTLOOK:

- Each type of gradient elution affect the adsorption isotherms uniquely.
- Elution technique improves retention and the cycle times, selectivity.

### Reference:

- [1] Qamar, S., Rehman, N., Carta, G., Seidel-Morgenstern, A. (2020). Analysis of gradient elution chromatography using the transport model. Chem. Eng. Sci. 115809.
- [2] N. Rehman; Abid, M., S. Qamar, "Numerical approximation of nonlinear and the nonequilibrium model of gradient elution chromatography"-Journal of Liquid Chromatography & and Related T.